

# NEUTRAL PION NUMBER FLUCTUATIONS AT HIGH MULTIPLICITY IN pp-INTERACTIONS AT 50 GeV

(SVD-2 Collaboration)

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The results of pion fluctuation measurements in SERP-E-190 experiment (project Thermalization) with 50 GeV proton beam irradiation of the liquid hydrogen target at SVD-2 setup are presented. The photons are detected in the electromagnetic calorimeter. MC modeling of photon detection has shown the linear dependence between number of photons in the calorimeter and the average number of neutral pions. Neutral pion number  $N_0$  distributions for each total number of particles in an event  $N_{tot} = N_{ch} + N_0$  are obtained after making corrections on the setup acceptance, triggering and efficiency of the event reconstruction. The scaled variance of neutral pion fluctuations,  $\omega = D / \langle N_0 \rangle$ , is measured. The fluctuations increase at  $N_{tot} > 22$ . According to quantum statistics models it may indicate for the approaching to pion condensate conditions for high pion multiplicity in the system. This effect have been observed for the first time.

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## I. INTRODUCTION

The SERP-E-190 experiment (project Thermalization) is carried out at upgraded setup SVD-2 (Spectrometer with Vertex Detector),

which is irradiated with 50 GeV proton beam from U-70 IHEP (Protvino) accelerator. The setup is equipped with a liquid hydrogen target, a microstrip silicon vertex detector (VD), a drift tube tracker, magnetic spectrometer, Cherenkov counter and an electromagnetic calorimeter for photon detection (DEGA) [1]. Project Thermalization is aimed at studying processes with high

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multiplicity in pp-interactions, which are one of fundamental regions of hadron physics. It is not possible to describe them with perturbative QCD. The theory gives only a qualitative picture of these processes. The multiplicity distribution at 50 GeV was measured earlier [2] up to the number of charged particles  $N_{ch}=16$  with average number of charged particles at this energy  $\langle N_{ch} \rangle = 5.3$ . The kinematical limit for the total number charged and neutral particles is  $N_{tot}=56$ . The data for  $N_{ch} = 4 \div 22$  and for  $N_{tot} = 4 \div 31$  are presented in this work. Collective effects can occur in the events with the multiplicity by several times higher than the average one: the large fluctuations of charged and neutral pion numbers, as result of formation pion condensate, formation of jets with identical pions, the so-called Bose-Einstein multiparticle effect, formation of ring events as result gluon hadronization, which are emitted out by partons in the nuclear environment (Cherenkov radiation analog) and others. The SVD-2 data allows one to check and develop various models of multiparticle production with  $N_{tot} \gg \langle N_{tot} \rangle$ .

M. I. Gorenstein and V. V. Begun [3] [4] have shown that at the approach of the pion system to Bose-Einstein condensate conditions (BEC) the neutral pion number fluctuations are increasing in accordance with the model based on quantum statistics. These fluctuations can be detected by the scaled variance,  $\omega$ , which is defined as the ratio of variance  $D$  for neutral pion number distribution  $N_0$  and average  $\langle N_0 \rangle$ ,

$$\omega = D / \langle N_0 \rangle.$$

The value of  $\omega$  rising with increasing of the total particle number,  $N_{tot} = N_{ch} + N_0$ , depends on temperature and energy density of pion system.

A part of E-190 data is used in this paper to search for pion number fluctuations. Numbers of charged particles,  $N_{ch}$ , and photons,  $N_\gamma$ , in each event are detected. These values are corrected on the setup acceptance and reconstruction efficiency by means of modeling. Simulation has allowed getting the neutral pion number,  $N_0$ , in each event also. Numbers of events,  $N_{ev}(N_0, N_{tot})$ , are measured here with corrections on various losses. For the analysis of the data at different  $N_{tot}$  relative values of  $n_0 = N_0/N_{tot}$  and  $r_0 = N_{ev}(N_0, N_{tot})/N_{ev}(N_{tot})$  are used. Thus  $n_0$  is changed in the range of  $0 \div 1$  and the sum of

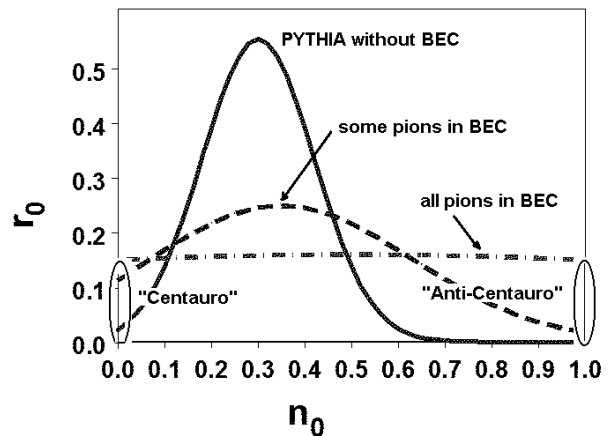


FIG. 1: Distributions  $r_0$  for normalized multiplicity of neutral pions in QCD model and when the system approaches to BEC.

all  $r_0$  is equal to 1 for each  $N_{tot}$  (normalization condition). The Fig. 1 qualitatively illustrates the behaviour of value  $r_0$  for three cases: a) the generation of events with PYTHIA5.6 program, b) the pion system in which some pions drop out into condensate, c) all pions are in the BEC condition. Each distribution is characterized by average,  $\langle n_0 \rangle$ , and by standard deviation,  $\sigma$  for a Gaussian fit.

## II. SIMULATION OF NEUTRAL PION DETECTION

Calorimeter DEGA at SVD-2 setup detects the events with photons from neutral pions decay. Registration of all  $\pi^0$  in the event is not possible because of limited DEGA aperture and the threshold on photon detection energy. But  $\pi^0$  reconstruction efficiency can be estimated by means of simulation. Using PYTHIA5.6 code  $10^6$  events (MC) are simulated for  $pp \rightarrow X$  inelastic interactions at 50 GeV. Only the events with  $N_{ch} \geq 4$  are analyzed. The photon detection efficiency is assumed to be equal to 1 if photon hits DEGA and its energy is greater than 100 MeV. Practically all photons are the product of  $\pi^0$  decays (95%), 37% of them give two gammas signal in DEGA and 18% of  $\pi^0$  result in one photon signal. Fig. 2 shows the dependence of pion number in event,  $N_0$ , on number of photons in DEGA,  $N_\gamma$ . It is clear that there is no unique connection between

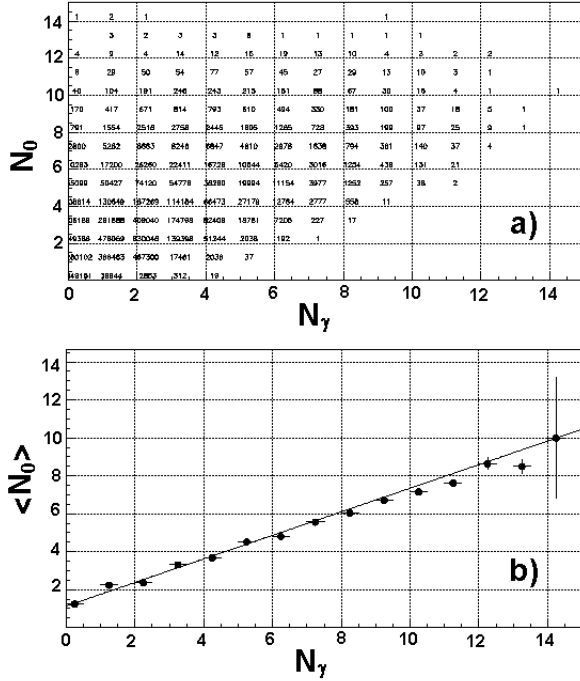


FIG. 2: a) The dependence of the pions number in MC events on photons number detected in DEGA, b)  $\langle N_0 \rangle$  and  $N_\gamma$  correlation

$N_\gamma$  and  $N_0$ . (Fig. 2a). Instead each  $N_\gamma$  is associated with some number of  $N_0$  and there is a linear correlation between average  $\langle N_0 \rangle$  and  $N_\gamma$  (Fig. 2b). So relation between the number of events  $N_{ev}(N_\gamma, N_{ch})$  and  $N_{ev}(N_0, N_{ch})$  can be found from this analysis. In Fig. 2c multiplicities distributions for pions and photons in DEGA are presented. The form of these distributions is similar except the area of small multiplicity.

Values  $n$  and  $r$  are calculated for MC events. Then the dependence of  $r$  versus  $n$  has been fitted with Gaussian. In Fig. 3a the fitted parameters  $\langle n_0 \rangle$  and  $\langle n_\gamma \rangle$  on  $N_{tot}$  are presented, where  $N_{tot} = N_{ch} + N_0$  for  $\pi^0$  and  $N_{tot} = N_{ch} + N_\gamma$  for photons. Standard deviations,  $\sigma$  of Gaussians, are presented in Fig. 3b too. The normalized dispersion,  $\omega = \sigma^2 * N_{tot} / \langle n \rangle$  is shown in Fig. 3c. The value  $\omega$  decreases for photons, but remains near the constant for pions in the full area of  $N_{tot}$  changes.

### III. PHOTON AND CHARGED PARTICLES RECONSTRUCTION

The calorimeter DEGA contains  $42 \times 32 = 1344$  elements from lead glass blocks with PM. The calibration of DEGA is carried out with irradiation of each element center by 15 GeV electron beam. Almost all (98%) energy of electromagnetic shower from the photon is located in the cell  $(3 \times 3)$  elements. Photon reconstruction consists in the searching of  $(3 \times 3)$  signal clusters and analyzing them with criteria for photon. The present work comprises  $\sim 5 \times 10^5$  events of pp interaction. The analysis of the electromagnetic showers has led to the following results: average photon number in the event is  $\langle N_\gamma \rangle = 3.0$  (Fig. 4), their average energy is  $\langle E_\gamma \rangle = 2.8$  GeV (Fig. 5b), the minimum energy of photon detection is equal to 100 MeV.

For the charged tracks reconstruction the data only from VD have been used. Because of various losses the corrections of charged particle number are essential for measurements of pion fluctuations. The correction for the setup acceptance and the particle reconstruction efficiency is made by means of the apparatus performance simulation. The obtained weights have shown the contribution of events with a different true number of charged tracks into the event sample with the reconstructed multiplicity. The details of this procedure are presented in [5]. In the present work the number of events with measured  $N_{ch}$  is distributed on event samples with restored value  $N_{ch}$  according to these weights.

Topological cross sections for pp-interactions at 50 GeV were measured in experiment with Mirabelle bubble chamber [2]. Taking into account that data topological cross sections for  $10 \leq N_{ch} \leq 24$  had been obtained in [5]. The present data are obtained with suppression of small charged multiplicity events ( $N_{ch} < 8$ ) with trigger conditions. Therefore the charged multiplicity distribution has been corrected to lead to the distribution received in [2] [5].

Fig. 5 shows charged multiplicity distributions after corrections. It is necessary to stress that the change of the event number for  $N_{ch}$  after introduction of corrections also leads to the change of the event number for  $N_\gamma$ . So, the distribution for  $N_\gamma$  in Fig. 5 differs from the similar

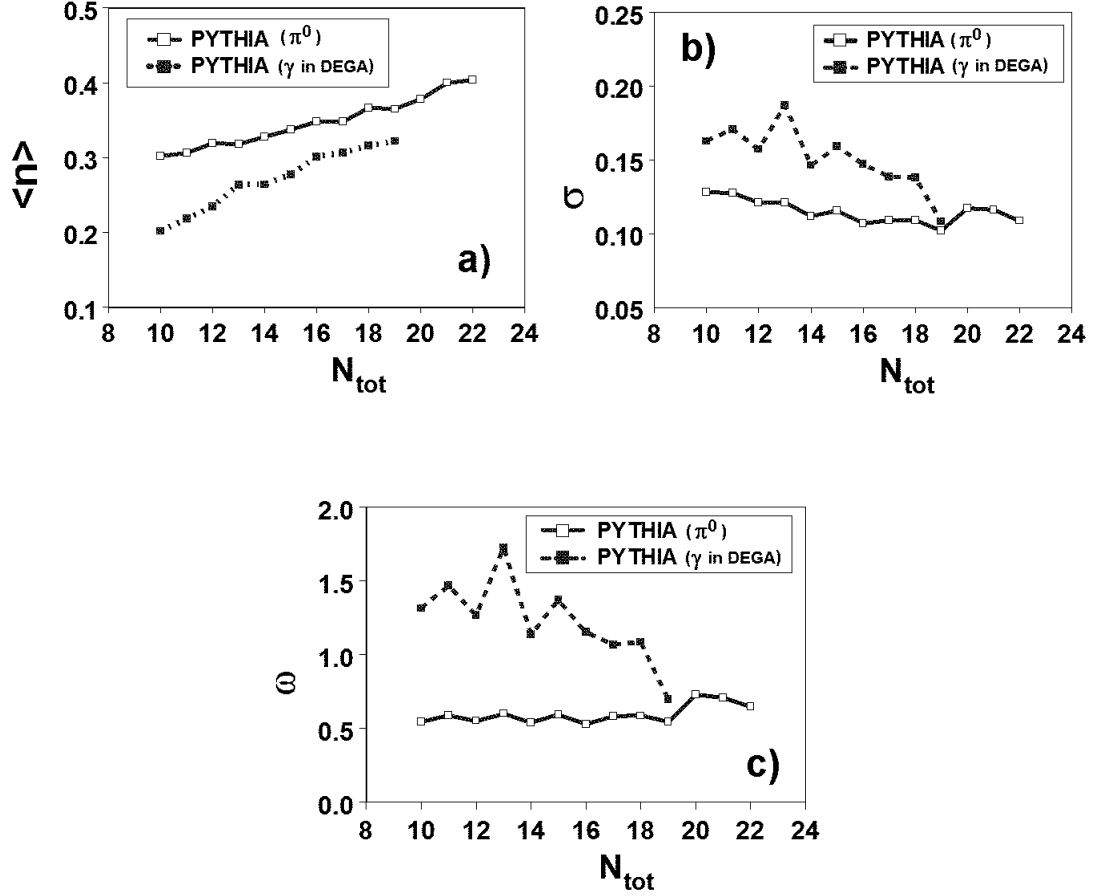


FIG. 3: a) Average  $\langle n_0 \rangle$ ,  $\langle n_\gamma \rangle$ ; b) standard deviation  $\sigma$  and c) scaled variance  $\omega$  dependence on  $N_{\text{tot}}$  (see text) for MC events.

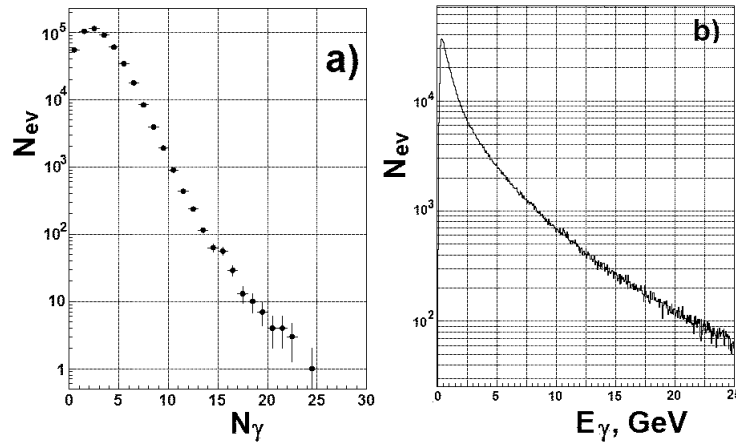


FIG. 4: a) Photon multiplicity distribution; b) photon energy distribution for MC events.

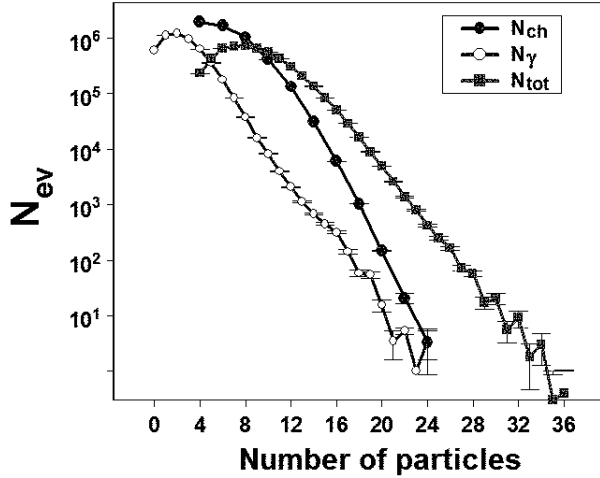


FIG. 5: Distributions of corrected  $N_{ch}$ ,  $N_\gamma$  and  $N_{tot} = N_{ch} + N_\gamma$ .

distribution in Fig. 4a for observable event numbers.

#### IV. NEUTRAL PION FLUCTUATION MEASUREMENTS

Thus we have corrected event numbers  $N_{ev}(N_\gamma, N_{ch})$ . Then two-dimensional  $N_{ev}(N_\gamma, N_0)$  distributions for MC events (see Fig. 2) are used to recover event numbers  $N_{ev}(N_0, N_{ch})$ . We have introduced notations  $i=N_\gamma$ ,  $j=N_0$  and  $N_{ev}(N_\gamma, N_0) = N_{ev}(i, j)$ . For each  $N_{ch}$  matrix of coefficients  $c_{ij} = N_{ev}(i, j)/N_{ev}(i)$  is calculated, where  $N_{ev}(i) = \sum_j N_{ev}(i, j)$ . Event number  $N_{ev}(N_\gamma, N_{ch})$  is decomposed in sums of events with various  $N_0$ ,  $N_{ev}(i, j) = c_{ij} * N_{ev}(i)$  at  $N_{ch}=\text{const}$ . Normalization condition  $\sum_j c_{ij}=1$  is satisfied. Resulting sum  $N_{ev}(j) = \sum_i N_{ev}(i, j)$  at  $N_{ch}=\text{fix}$  is the analog of event number  $N_{ev}(N_\gamma, N_{ch})$ , but for pions.

The simulation by PYTHIA5.6 allows to obtain  $c_{ij}$  for  $N_\gamma \leq 10$  and  $N_{ch} \leq 14$  only because of limitation of the MC events statistics. Regularities of factors  $c_{ij}$  are used to continue them to  $N_\gamma \geq 10$  and  $N_{ch} \geq 14$  region. Fig. 6a illustrates the dependence of  $c_{ij}$  factors on  $N_0$  for various  $N_\gamma$  and  $N_{ch}$ . The form of these distributions slightly depends on  $N_\gamma$  and  $N_{ch}$ , but their average  $\langle N_0 \rangle$  increases with  $N_\gamma$ . The dependence of the average  $\langle N_0 \rangle$  and standard deviation (rms)

on  $N_\gamma$  are shown in Fig. 6b. After fitting it by linear dependence the coefficients  $c_{ij}$  for  $N_\gamma \geq 10$  and  $N_{ch} > 14$  are calculated and the full sample of  $N_{ev}(N_{tot}, N_{ch}, N_0)$  is obtained, which is used then to determine pion fluctuation.

As mention before we have used scaled variables  $n_0$  and  $r_0$  (see Introduction):  $n_0 = N_0/N_{tot}$  and  $r_0(n_0) = N_{ev}(N_0, N_{tot})/N_{ev}(N_{tot})$ , where  $N_{tot} = N_0 + N_{ch}$ . Function  $r_0(n_0)$  are shown in Fig. 7 for every  $N_{tot} > 10$ . All distributions are fitted with Gaussian function. The dependence of the fitting parameters is presented in Fig. 8. The data in the intervals (26, 27, 28) and (29, 30, 31) are combined due to small statistics.

One can see that the measured average  $\langle n_0 \rangle$  (Fig. 8) coincide with the same values for the neutral pions from MC events at  $N_{tot} > 12$ . In the gluon dominance model (MGD) [6] neutral pions average dependence on  $N_{tot}$  has been received by analytical way. This dependence is also presented in Fig. 8 and illustrates quite good agreement with the experimental data at  $N_{tot} > 14$ . The average  $\langle n_\gamma \rangle$  is also shown. The measured standard deviations,  $\sigma$  (Gaussian), (Fig. 8b) have shown the qualitative agreement with MC model only for  $N_{tot} < 22$ . The measured values  $\sigma$  increase at higher  $N_{tot}$ .

The theoretical prediction of scaled variance  $\omega$  behavior (in our case  $\omega = D(N_0)/\langle N_0 \rangle = \sigma^2 * N_{tot}/\langle n_0 \rangle$ ) is given in [3]. The analysis has been done for three energy densities of the pion system at the approach to the Bose-Einstein condensate condition (pion condensate) (Fig. 9). Our experimental data (Fig. 9b) have confirmed assumption on the BEC formation in pion system at  $N_{tot} > 22$  in pp-interactions at 50 GeV.

#### V. CONCLUSION

Measurements of the charged and neutral pions number in the events with high multiplicity in pp-interactions at 50 GeV (experiment SERP-190, SVD-2 setup) together with MC analysis led to the following results:

- The average number of neutral pions in the event is proportional to the photons number detected in DEGA calorimeter that allows one to extract pion number fluctuations from photon number fluctuations.

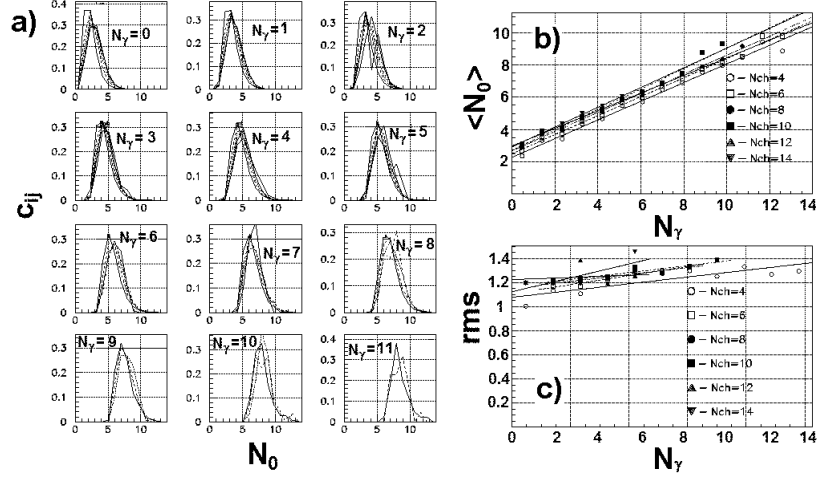


FIG. 6: a) The dependence of  $c_{ij}$  factors on  $N_0$  for various  $N_\gamma$  and  $N_{ch}$ , b) fitting parameters:  $\langle N_0 \rangle$  and standard deviation (rms) as function of  $N_\gamma$  for various  $N_{ch}$ .

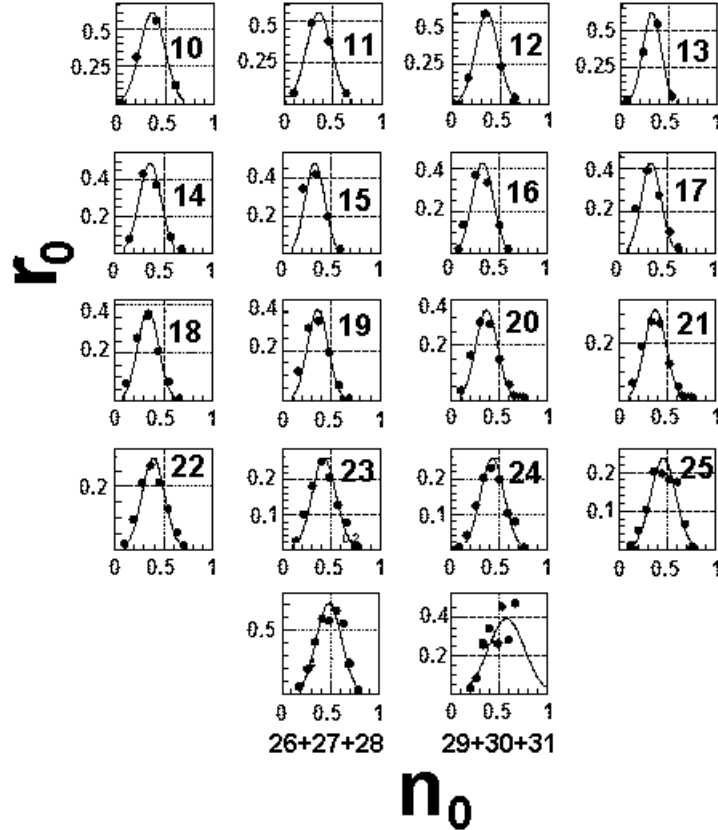


FIG. 7: Scaled neutral pions number  $n_0$  distributions for various  $N_{tot}$  (are specified by number).

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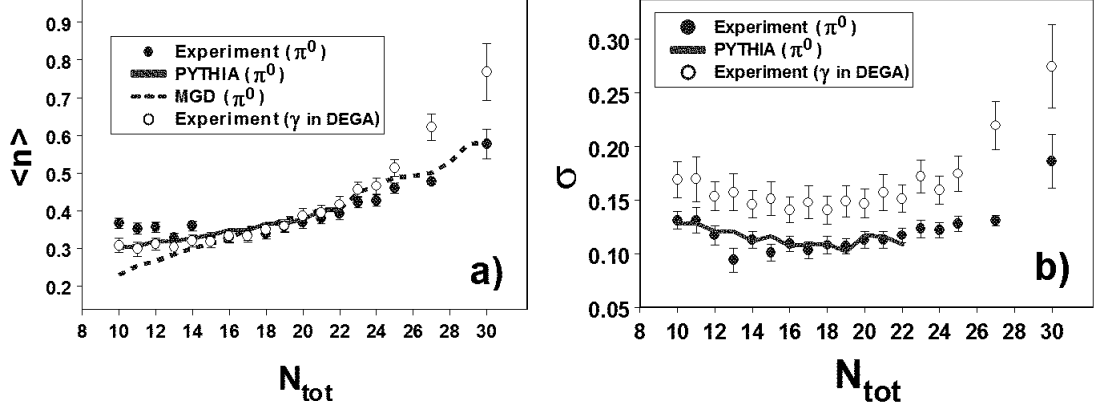


FIG. 8: Fitted parameters of neutral pions number and photons number distributions for experimental data and C events as function of  $N_{tot}$ . For neutral pions  $N_{tot} = N_{ch} + N_0$ , for photons  $N_{tot} = N_{ch} + N_\gamma$ .

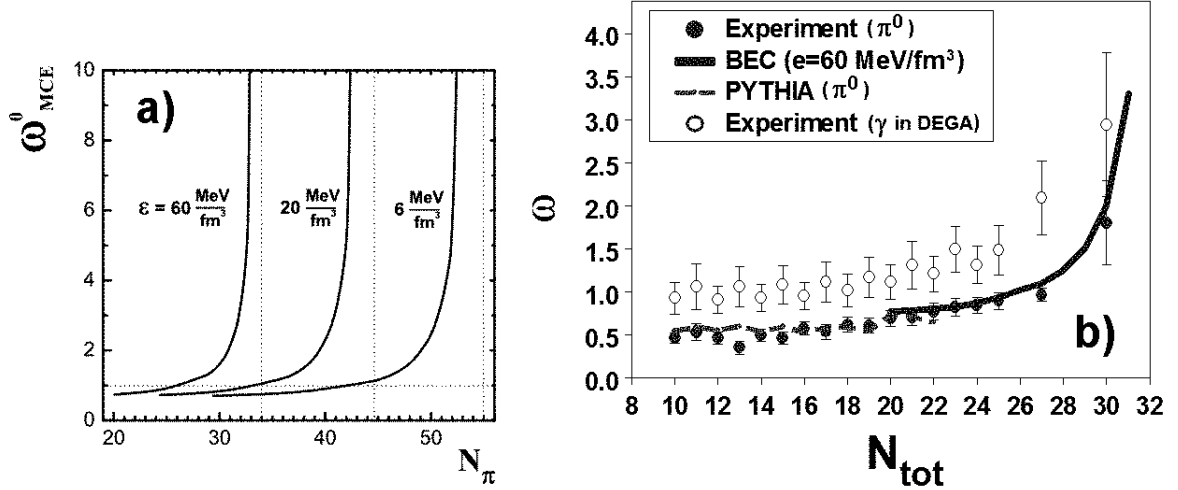


FIG. 9: Scaled variance  $\omega$  as function of  $N_{tot}$  [3] and b) the result of the present measured of  $\omega$  for neutral pions and photons.  $N_{tot} = N_{ch} + N_0$  for neutral pions,  $N_{tot} = N_{ch} + N_\gamma$  for photons.

- It is convenient to present data in the scaled form:  $n_0 = N_0/N_{tot}$  and  $r_0(n_0) = N_{ev}(N_0, N_{tot})/N_{ev}(N_{tot})$  with interval  $n_0$  is equal to  $0 \div 1$ .
- The corrections for limited aperture VD, trigger action and efficiency of data processing system have been introduced to the data.
- The function  $r_0(n_0)$  is fitted with Gaussian function and values  $\langle n_0 \rangle$ ,  $\sigma$  and scaled variance  $\omega = D/\langle N_0 \rangle$  are derived. They have shown the qualitative

agreement with the same values received for PYTHIA5.6 code at  $N_{tot} < 22$ .

- Pion number fluctuations increase at  $N_{tot} > 22$ , that indicates approaching to pion condensate conditions for the high multiplicity pion system according to GCE, CE, MCE models [3] [4].
- This effect has been observed for the first time.

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